

**SUMMARY NOTES**

# **MEASURES OF DISPERSION**

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# Illustrations

- Consider IQs of 2 groups of students , 10 per group. Each group having mean IQ of 100
- Group 1: range of 70-140
- Group 2; range of 90-120
- Latter group appear more homogenous than the other, and thus students would find it easier comparatively to understand lectures taught?
- Group A appear more varied? More conclusions which central tendency may not give
- Dispersion= 'away' from the centre, unlike central tendency which connotes 'towards the centre'

# Introduction

- Spread
- Disperse
- Variability
- Scatter
- More useful than Central tendency
- Why are there differences in observations
- How far is data  $x$  from the center of the data

# Some measures of dispersion

- Range
- Quartiles
- Mean deviation
- Variance
- Standard deviation: mostly used
- Coefficient of variation-sample variance/mean

# Possible causes of variation

- Random measurement errors
- Instrument measurement errors
- Procedural errors
- Observer error
- Biological variability
  - Intra or
  - inter individual variability

# Range, quartiles

- Range: Maximum-minimum  
Highest-lowest

Quartiles: Using the data provided

Step 1: arrange in increasing order of magnitude

Step 2: compute the cumulative frequencies

Q1=1<sup>st</sup> quartile= cumulative frequency  
containing 25% of one quarter of total  
frequency ( $n/4$ )

# Calculation of Qs

- $Q2 = 2^{\text{nd}}$  quartile = 50% =  $n/2$  = median
- $Q3 = 75\%$  = three quarters
- Exercise: using the data provided
- Identify the class interval containing  $Q1$ ,  $Q2$  and  $Q3$
- Calculate the precise values of  $Q1$ - $Q3$

# Calculating precise values of Qs

- $Q1 = x_0 + \frac{n/4 - F_c}{F_1} * L$

$X_0$  = lower limit of class interval in which  $n/4$  falls

$F_c$  = cumulative frequency in the immediately preceding class interval

$F_1$  = frequency in the interval where  $n/4$  falls

$L$  = class interval

$Q_2$  is similar in formula to  $Q_1$  but  $2 * n/4$

$Q_3$  is similar in formula to  $Q_1$  but  $3 * n/4$

# Semi Interquartile range (SIR)

- Inter-quartile range= $Q3-Q2$
- Semi interquartile range or quartile deviation  
=average of distance of  $Q1$  to  $Q2$  and  $Q2$  to  $Q3$ = half of inter-quartile range above
- SIR is employed when the
  - Median is the central location used
  - Distribution is skewed
  - Extremes are indeterminate

# Mean deviation, Variance, Standard deviation

- Mean deviation =  $E(X - \text{mean})/n$
- $X$  is the midpoint
  
- Variance =  $E(X - \text{mean})^2/n - 1$
- $N$  for a population rather than sample ( $n$ )
- Standard deviation = square root of variance
- Add  $f$  to the formula (numerator) in case of grouped data with frequencies

# Calculating variance and standard deviation

- Depending on the set of data given, whether grouped or not, class or no class interval
  - Draw the frequency distribution table
  - Calculate the mean
  - Find midpoint
  - Use the formular after creating the following columns
    - Midpoint-mean
    - (Midpoint-mean)<sup>2</sup>
    - (midpoint-mean)f
    - (midpoint-mean)<sup>2</sup>f

# Assignment

- Write the formular for calculating
  - Mean
  - Mean deviation
  - Variance
  - Standard deviation
- Using the set of data provided, compute the
  - Semi interquartile range
  - Sample mean
  - Variance
  - Standard deviation